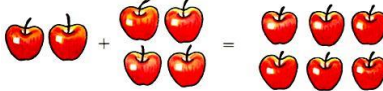
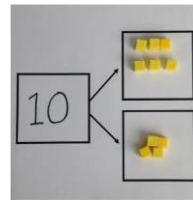



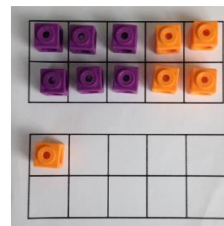
Addition


Year 1

Pictures
 $2 + 4 = 6$


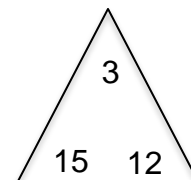
Part Whole
 $10 = 6 + 4$


Number lines
 $5 + 12 = 17$


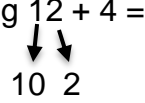
Tens frames
 $6 + 5 = 11$


Number bonds


Linked number sentences
 $2 + 3 = 5$
 $3 + 2 = 5$

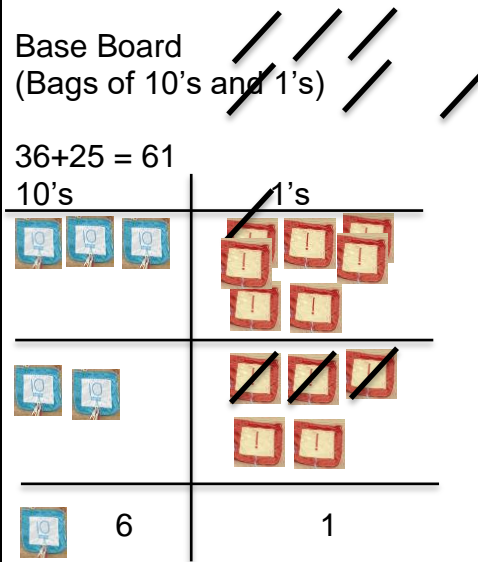
Represent and use number bonds and related subtraction facts within 20
 $12 + 3 = 15$
 $3 + 12 = 15$
 $15 - 12 = 3$
 $15 - 3 = 12$


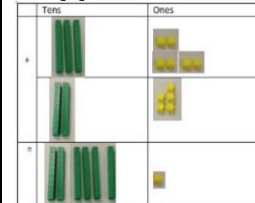
Add and subtract one-digit and two-digit numbers to 20, including zero

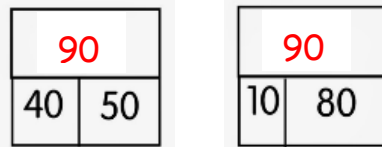
Partitioning $12 + 4 =$


Year 2

Adding ten to any two digit number to apply understanding of place value
 Add 2 two digit numbers

Base Board
 (Bags of 10's and 1's)
 $36 + 25 = 61$


Tens and ones
 $36 + 25$


Part-Part-Whole


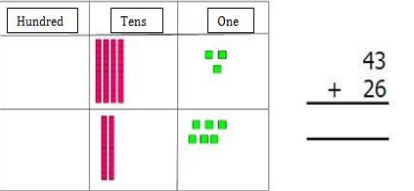
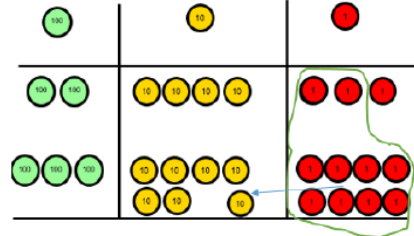
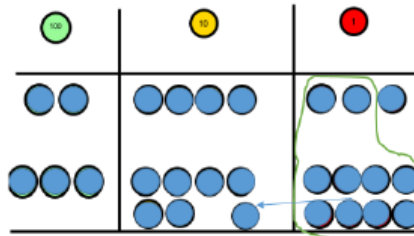
Recall and use addition and subtraction facts to 20 fluently, and derive and use related facts up to 100
 $7 + 2 = 9$
 $70 + 20 = 90$

Add numbers using concrete objects, pictorial representations, and mentally, including:

- + a two-digit number and ones
 $36 + 7 =$
- + a two-digit number and tens
 $28 + 40 =$
- + two two-digit numbers
 $38 + 27 =$
- + adding three one-digit numbers
 $3 + 5 + 7 =$

Year 3

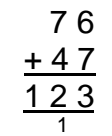
Adding using:
 -Near doubles e.g. $5 + 6$
 Bridging $8 + 5$
 -Compensating $23 + 9$
 (+10 - 1)

Column addition with dienes or PV counters and PV chart




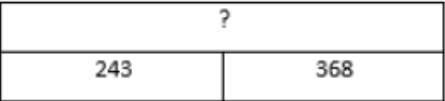
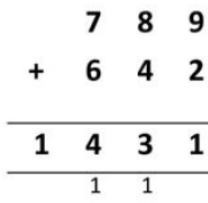
Add a three-digit number and ones
 $467 + 8 =$

Add a three-digit number and tens
 $637 + 50 =$

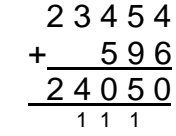
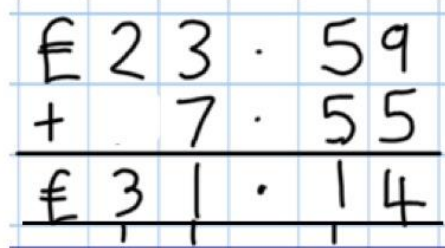
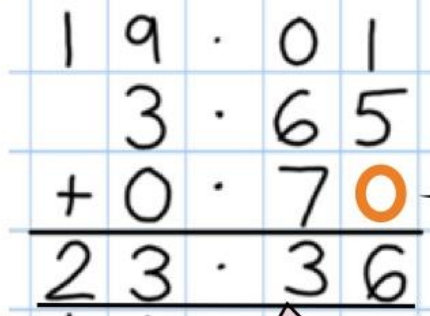
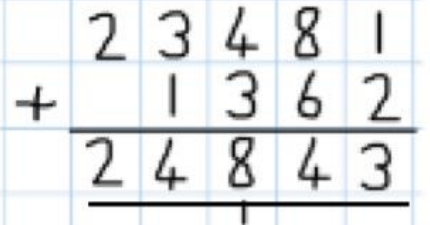
Add a three-digit number and hundreds
 $458 + 500 =$

Add numbers with up to three digits, using formal written methods of column addition

(Make sure the one ten carried across is marked underneath the line, and is not crossed off when counted)

Year 4

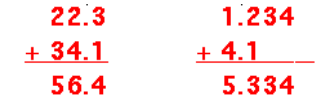
Add numbers with up to 4 digits using the formal written methods of column addition where appropriate



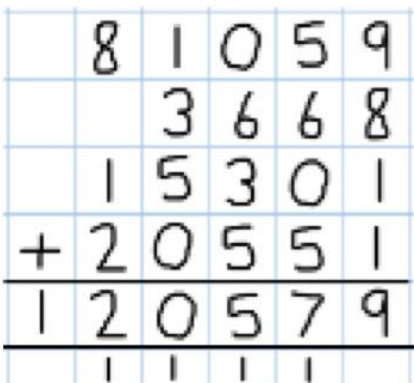
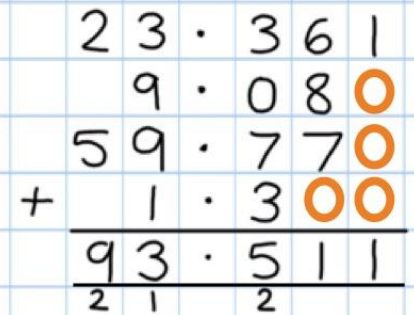
Year 5

Add and subtract whole numbers with more than 4 digits, including using formal written methods (columnar addition and subtraction)






Add and subtract numbers mentally with increasingly large numbers

Year 6



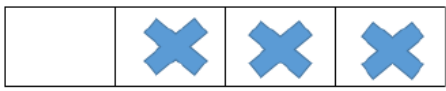
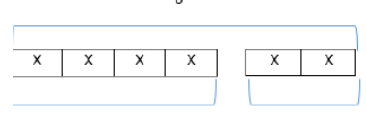


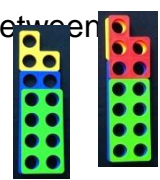
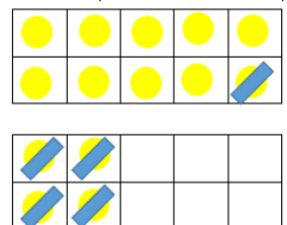
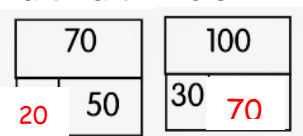
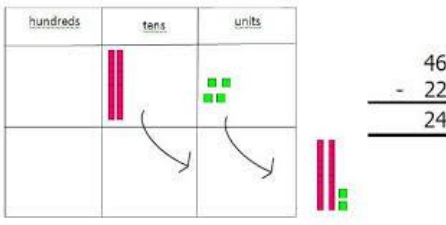
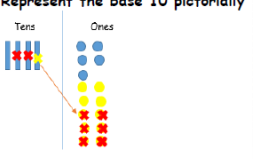
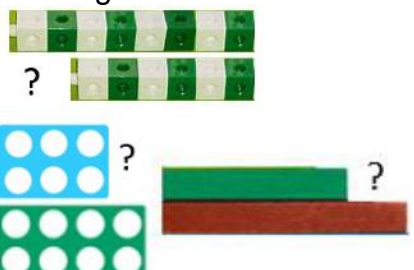
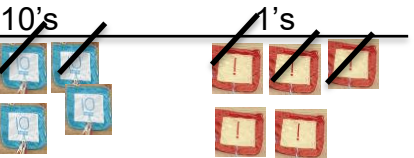
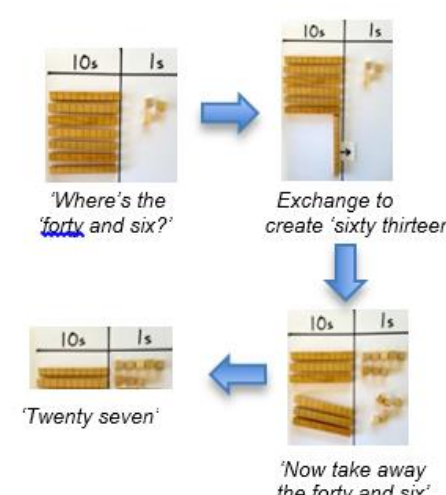
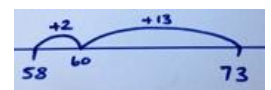
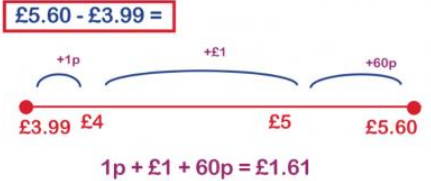
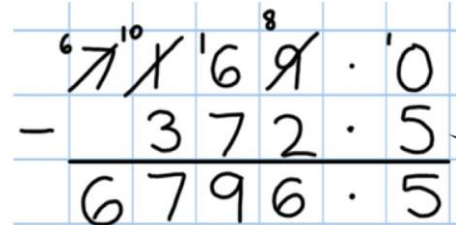
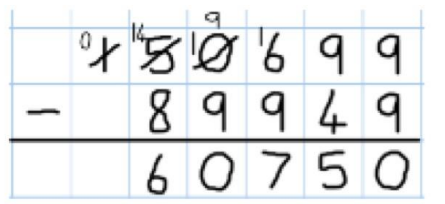
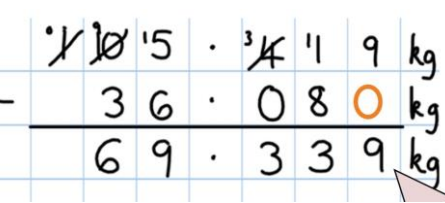
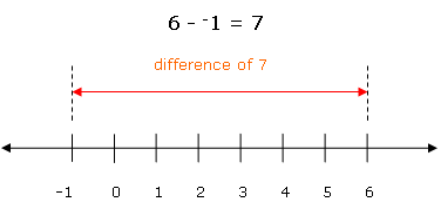
Pupils practice addition, for larger numbers, using the formal written methods of column addition


Building up to adding several numbers using written method, including zeroes as place holders:








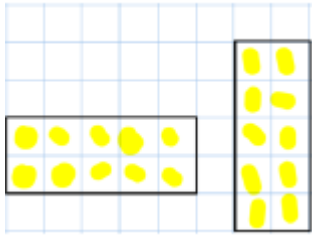
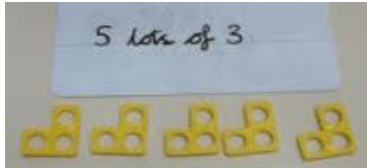
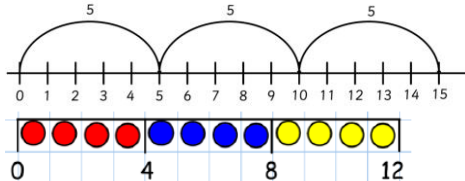


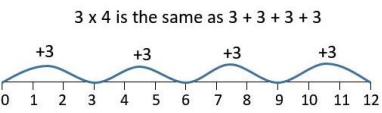


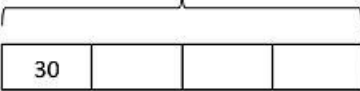
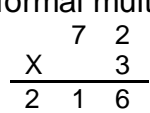
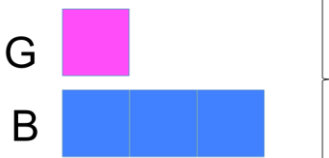
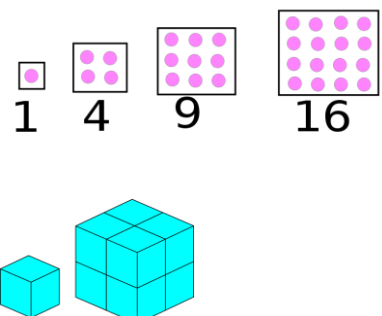
Use their knowledge of the order of operations to carry out calculations involving the four Operations
 $3.5 + 1.5 \times 10 =$

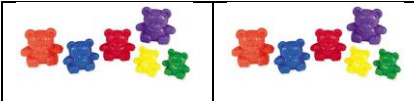
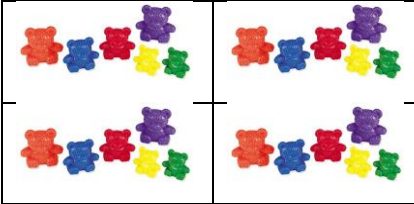
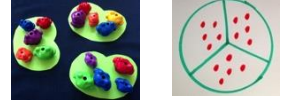



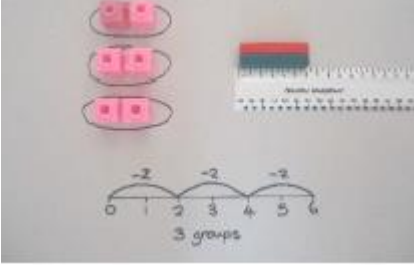
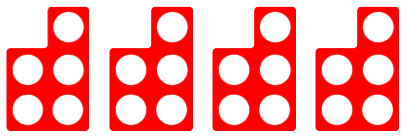
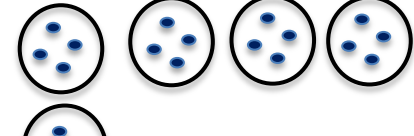
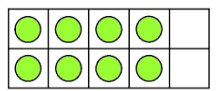
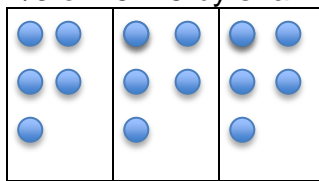
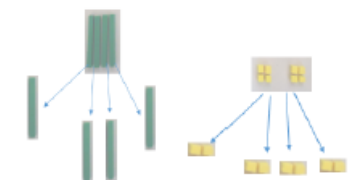


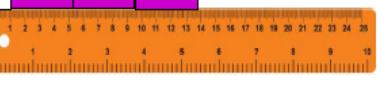
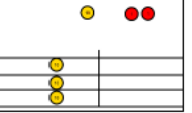
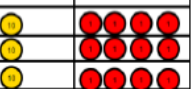
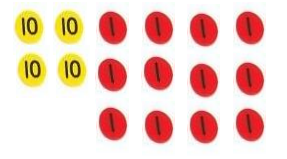
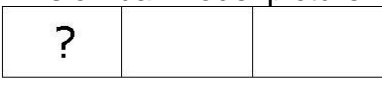
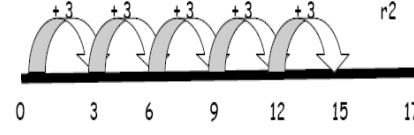



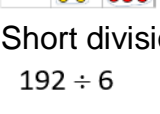
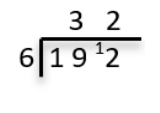
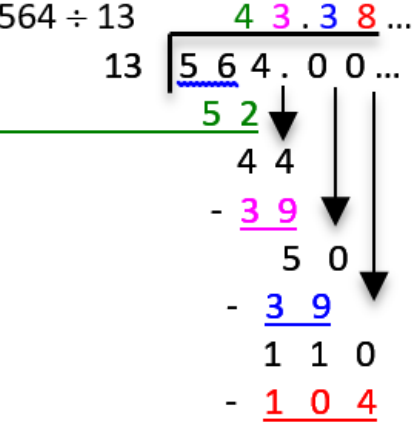
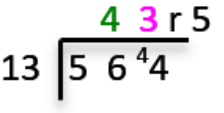
To solve problems using the inverse:


Subtraction








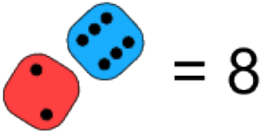

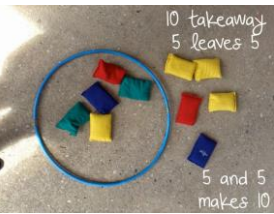



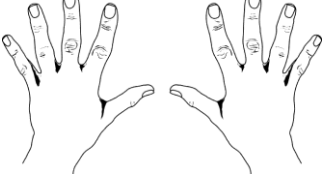

Year 1	Year 2	Year 3	Year 4	Year 5	Year 6
<p>take away, distance between, difference between, more than and less than</p>  <p>Multilink towers $5 - 4 = 1$</p> <p>6 less than 10 is 4</p>  <p>Use of the bar model:</p>   <p>Count out, then count how many are left. $7 - 4 = 3$</p>   <p>Difference between 13 and 8 $13 - 8 = \underline{\quad}$ $8 + \underline{\quad} = 13$</p>  <p>Children to present the ten frame pictorially</p> 	<p>Part-Part-Whole</p>  <p>2 digit – 2 digit</p>  <p>46 - 22 --- 24</p> <p>Represent the base 10 pictorially</p>  <p>Difference with practical resources, children recording drawing</p>  <p>Recall and use subtraction facts to 20 fluently, and derive and use related facts up to 100 e.g. $12 - 4 = 8$ $120 - 40 = 80$</p> <p>Base Board (Bags of 10's and 1's) $45 - 22 = 23$</p>  <p>Subtract numbers using concrete objects, pictorial representations, and mentally, including:</p> <ul style="list-style-type: none"> a two-digit number and ones a two-digit number and tens two two-digit numbers 	<p>Column subtraction with dienes and PV chart</p> <p>Taking away and exchanging, $73 - 46$</p>  <p>'Where's the forty and six?'</p> <p>Exchange to create 'sixty thirteen'</p> <p>'Twenty seven'</p> <p>'Now take away the forty and six'</p> <p>Counting up to find change and the difference. Difference between 73 – 58 by counting up, $58 + \underline{\quad} = 73$</p>  <p>Subtract:</p> <ul style="list-style-type: none"> a three-digit number and ones a three-digit number and tens a three-digit number and hundreds <p>Subtract numbers with up to three digits, using formal written methods of columnar addition and subtraction</p> $\begin{array}{r} 2\ 3\ 1 \\ 3\ 4\ 4 \\ - 1\ 8\ 7 \\ \hline 1\ 5\ 7 \end{array}$	<p>Counting up to find change</p> <p>$£5.60 - £3.99 =$</p>  <p>$1p + £1 + 60p = £1.61$</p> <p>Subtract numbers with up to 4 digits using the formal written methods of columnar addition and subtraction where appropriate</p> $\begin{array}{r} 1 \\ 2\ 3\ 1 \\ 2\ 3\ 4\ 4 \\ - 1\ 8\ 7 \\ \hline 2\ 1\ 5\ 7 \end{array}$ <p>Counting up on a number line to find complements to multiples of 10 or 100 to used for money, fractions, decimals and negative numbers.</p>	<p>Subtract whole numbers with more than 4 digits, including using formal written methods (columnar addition and subtraction)</p> <p>T Th Th H T O</p> $\begin{array}{r} 7\ 4\ 5\ 1\ 5\ 3\ 1\ 2 \\ - 2\ 2\ 6\ 2\ 3 \\ \hline 5\ 2\ 9\ 0\ 9 \end{array}$ <p>$213323 - 70 =$ $512893 + 300 =$ $819354 - 500 = 319954 + 100$</p> <p>Subtract numbers mentally or using written methods with increasingly large numbers including decimals:</p>  <p>11.74 - 11.18 33.3 - 32.71</p>	<p>Subtract numbers mentally and using formal written methods fluently.</p>   <p>Finding differences between positive and negative</p> <p>$6 - -1 = 7$</p>  <p>$22,964 - 7,483$ $3054 - 817 - 44$</p> <p>Carry out mental subtraction converting measures.</p> <p>$3200m - 1,65km$</p> <p>Subtract fractions with different denominators.</p> $\frac{8}{9} - \frac{2}{3}$

Multiplication

Year 1	Year 2	Year 3	Year 4	Year 5	Year 6																
<p>Counting in twos, fives and tens</p> <p>repeated addition $2 \times 3 = 2 + 2 + 2 =$</p>  <p>arrays</p> <p>multilink</p>  <p>numicon</p>  <p>$2 \times 5 = 5 \times 2$</p>  <p>solve one-step problems involving multiplication and by calculating the answer using concrete objects, pictorial representations and arrays with the support of the teacher.</p>	<p>Times Tables 2,5,10 and counting in 3s</p> <p>Arrays</p>  <p>$4 \times 6 = 24$ $6 \times 4 = 24$</p>  <p>Numicon</p>  <p>Repeated addition</p> <p>$5 \times 3 = 5 + 5 + 5 = 15$</p>  <p>Use of a bar model for a more structured method</p>  <p>Application of times tables facts</p>	<p>Times Tables: 4, 8 and 3</p> <p>Arrays / linked to area $5\text{cm} \times 2\text{cm} = 10\text{cm}^2$</p>  <p>Area = 10 cm^2</p> <p>Repeated addition</p> <p>3×4 is the same as $3 + 3 + 3 + 3$</p>  <p>Partitioning Method $13 \times 4 = (10 \times 4) + (3 \times 4)$</p>  <p>Make 23, 3 times. See how many ones, then how many tens</p>  <p>Bar model</p>  <p>$30 \times 4 = 120$</p> <p>3×23 $3 \times 20 = 60$ 20×3 $3 \times 3 = 9$ $60 + 9 = 69$</p> <p>23 $\times 3$ 69</p> <p>Short formal multiplication</p> 	<p>Times Table 6, 7,9,11,12</p> <p>Factors and multiples Use terminology 'factor', 'multiples; and 'product' e.g. $3 \times 4 = 12$ 3 and 4 are a factor pair for 12 (the product)</p> <p>Multiply numbers up to 4 digits by a two-digit whole number using the formal written method of short multiplication</p> <p>243 $\times 6$ 2058 1</p> <p>Bar Model to solve scaling problems</p>  <p>Multiplying by 0</p> <p>Multiply numbers by 10, 100 and 1000</p> <p>Multiplying and Dividing by 10, 100 and 1000</p> <table border="1" data-bbox="1537 1430 1932 1535"> <tr> <td>10 000</td> <td>1000</td> <td>100</td> <td>10</td> <td>1</td> <td>$\frac{1}{10}$</td> <td>$\frac{1}{100}$</td> <td>$\frac{1}{1000}$</td> </tr> <tr> <td></td> <td></td> <td></td> <td></td> <td></td> <td></td> <td></td> <td></td> </tr> </table> <p>Multiplying $\times 10$ digits move LEFT 1 space $\times 100$ digits move LEFT 2 spaces $\times 1000$ digits move LEFT 3 spaces</p> <p>Dividing $\div 10$ digits move RIGHT 1 space $\div 100$ digits move RIGHT 2 spaces $\div 1000$ digits move RIGHT 3 spaces</p>	10 000	1000	100	10	1	$\frac{1}{10}$	$\frac{1}{100}$	$\frac{1}{1000}$									<p>Multiply multi-digit numbers up to 4 digits by a two-digit whole number using the formal written method of long</p> <p>Long multiplication</p> <p>32 $\times 15$ 160 320 480</p> <p>Factors and multiples, prime numbers</p> <p>Squared and cubed numbers</p>  <p>Numbers $\times 100, 1000$ and $10,000$, including decimals.</p>	<p>Multiply multi-digit numbers up to 4 digits by a two-digit whole number using the formal written method of long</p> <p>469 $\times 32$ 1938 14070 15008</p> <p>Perform mental calculations, including with mixed operations and large numbers multiplication</p> <p>Multiplication of decimals using linked times tables facts. 0.6×7 0.08×9 15×6.1</p> <p>Common factors, common multiples and prime numbers</p> <p>Multiply one-digit numbers with up to two decimal places by whole numbers</p> <p>Short method</p> <p>21.8 $\times 3$ 65.4 2</p> <p>Use their knowledge of the order of operations to carry out calculations involving the four operations</p>
10 000	1000	100	10	1	$\frac{1}{10}$	$\frac{1}{100}$	$\frac{1}{1000}$														

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<p>Halving</p> <p>$10 \div 2 = 5$</p>  <p>Quarters</p> <p>$20 \div 4 = 5$</p>  <p>Sharing</p> <p>$15 \div 3 = 5$ in each group (sharing)</p>  <p>Link to fractions</p>   <p>Grouping</p> <p>$15 \div 3 = 5$ groups of 3 (grouping)</p>  	<p>Counting in 2,5,10 and 3.</p> <p>Division by grouping (numicon, or counting in groups), eg $20 \div 5$</p>   <p>(for numbers upto 20)</p> <p>Applying knowledge of halving (can be supported with a tens frame or numicon)</p>  <p>e.g. Half of 8 = 4 Half of 24 = 12 Half of 30 = 15</p> <p>$1/3$ of 15 = 5 by sharing</p>  <p>From a known fact, create a division fact e.g. $3 \times 5 = 15$ so $15 \div 5 = 3$ BUT $5 \div 15 \neq 3$</p> <p>$48 \div 4 = 12$</p>  <p>Start with the tens.</p>	<p>Counting on in groups mentally (using a number line, practical resources or numicon as required)</p> <p>$20 \div 3 = 6r2$</p>  <p>Use of lollipop sticks to form wholes</p>  <p>Use of Cuisenaire rods and rulers (using repeated subtraction)</p>  <p>$42 \div 3 = 14$</p>  <p>1. Make 42. Share the 4 tens between 3. Can we make an exchange with the extra 10?</p>  <p>Exchange the ten for 10 ones and share out 12 ones</p> <p>Long division with one digit using place value counters</p> $\begin{array}{r} 26 \\ 2 \overline{) 52} \\ - 4 \\ \hline 12 \\ - 12 \\ \hline 0 \end{array}$  <p>Division bar model picture</p>  <p>← 24 →</p> <p>$24 \div 3 = ?$</p>	<p>Mental Division with remainders</p> <p>How many groups of 3 in 17? e.g. $17 \div 3 = 5 r 2$</p>  <p>Long division – continuing to use the place value counters and recording:</p> $\begin{array}{r} 26 \\ 2 \overline{) 52} \\ - 4 \\ \hline 12 \\ - 12 \\ \hline 0 \end{array}$ <p>Dividing by 0</p> <p>Numbers $\div 10$ and 100.</p>	<p>Divide numbers up to 4 digits by a one-digit number using the formal written method of long and short division and interpret remainders appropriately for the context</p> <p>Long division (with remainders)</p> $\begin{array}{r} 2191 \\ 4 \overline{) 8764} \\ \underline{81} \\ 07 \\ \underline{07} \\ 00 \\ \underline{04} \\ 00 \\ \underline{00} \\ 00 \\ \underline{00} \\ 00 \\ \underline{00} \\ 00 \end{array}$ <p>$615 \div 5$</p>  <p>Step 1: make 615</p>  <p>Step 2: Circle your groups of 5</p>  <p>Step 3: Exchange 1H for 10T and circle groups of 5</p>  <p>Step 4: exchange 1T for 10ones and circles groups of 5</p>  <p>Short division (if needed)</p> $\begin{array}{r} 32 \\ 6 \overline{) 192} \\ \underline{18} \\ 12 \\ \underline{12} \\ 0 \end{array}$ <p>$192 \div 6 = 32$</p> <p>Record remainders as fractions and known decimals.</p> <p>Numbers $\div 100$, 1000 and 10,000, including decimals.</p>	<p>Divide numbers up to 4 digits by a two-digit whole number using the formal written method of long division, and interpret remainders as whole number remainders, fractions, or by rounding, as appropriate for the context</p> <p>$564 \div 13 = 43 r 5 = 43 \frac{5}{13} = 43.4$ (to 1dp)</p>  <p>Known multiplication facts: 13, 26, 39, 52, 65, ... $10 \times 13 = 130$, $20 \times 13 = 260$</p> <p>$564 \div 13 = 43 r 5 = 43 \frac{5}{13}$</p>  <p>Divide fractions by whole numbers</p> $\frac{9}{17} \div 3 = \frac{9}{17} \div \frac{3}{1} = \frac{9}{17} \times \frac{1}{3} = \frac{9 \times 1}{17 \times 3} = \frac{9}{51} = \frac{9 \div 3}{51 \div 3} = \frac{3}{17}$

EYFS

Basic Skills	Addition	Subtraction	Multiplication	Division
<p>Number recognition to 20</p>  <p>Match numeral to quantity (including Numicom tiles)</p>   <p>Ordering numbers to 20</p>  <p>Writing numbers (Rhyme cards)</p>  <p>1:1 correspondence, counting objects (deliberate pause)</p> <p>Count out given number or objects from larger group</p>	<p>Find total of 2 groups of objects by counting all of them</p>  <p>Number tracks</p>  <p>Counting on from the larger number</p>  <p>1 more (mentally counting on to the next number)</p> 	<p>Take away a number of objects from a group</p>  <p>Number tracks</p>  <p>Problem stories e.g. 5 dinosaurs, 2 were eaten by a T-Rex, how many are left?</p>  <p>1 less than (mentally counting back to the previous number)</p>	<p>Doubling</p>  <p>Fingers – same on both hands</p> 	<p>Sharing fairly</p>  <p>Finding half of a number of objects</p> 